

# ***Ultra high-energy cosmic ray production at the deceleration onset of the GRB outflow***

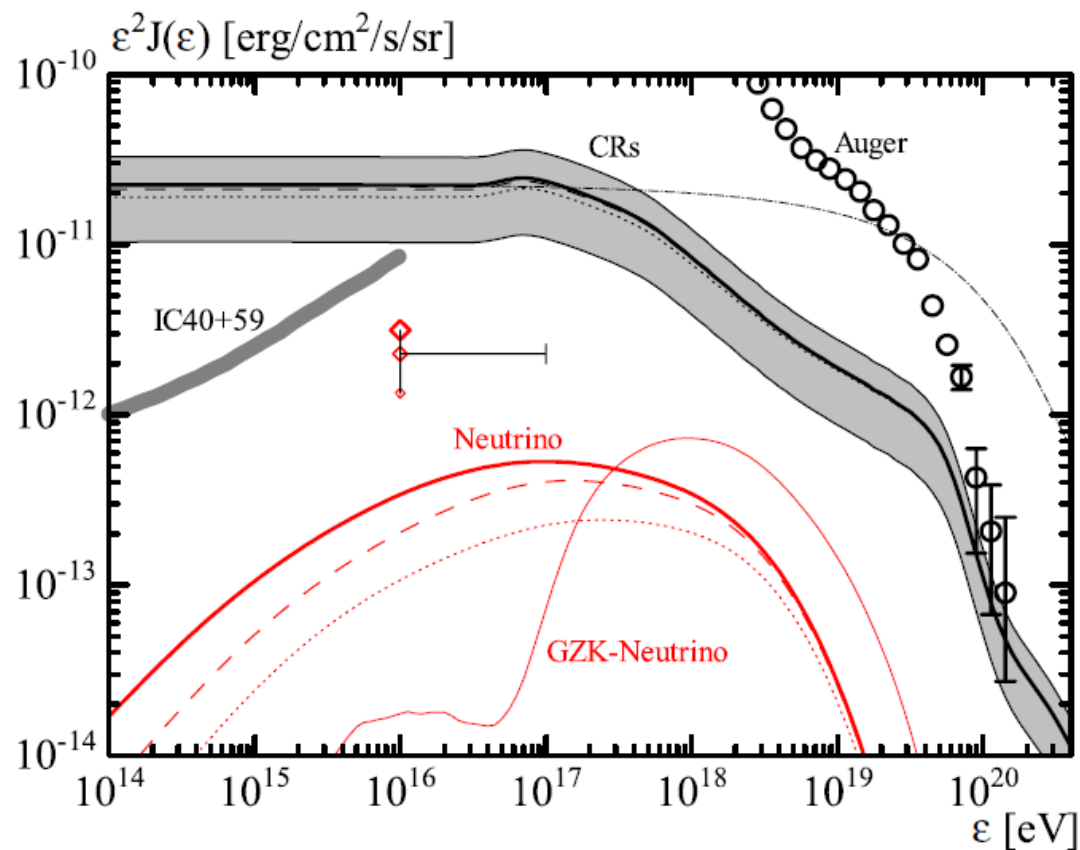
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# Ultra High-Energy Cosmic-Rays

**Power-law injection of protons ( $p = 2$ )**

**Even with  $f_{\text{CR}} \equiv \frac{L_{\text{CR}}}{L_{\gamma}} = 10$**

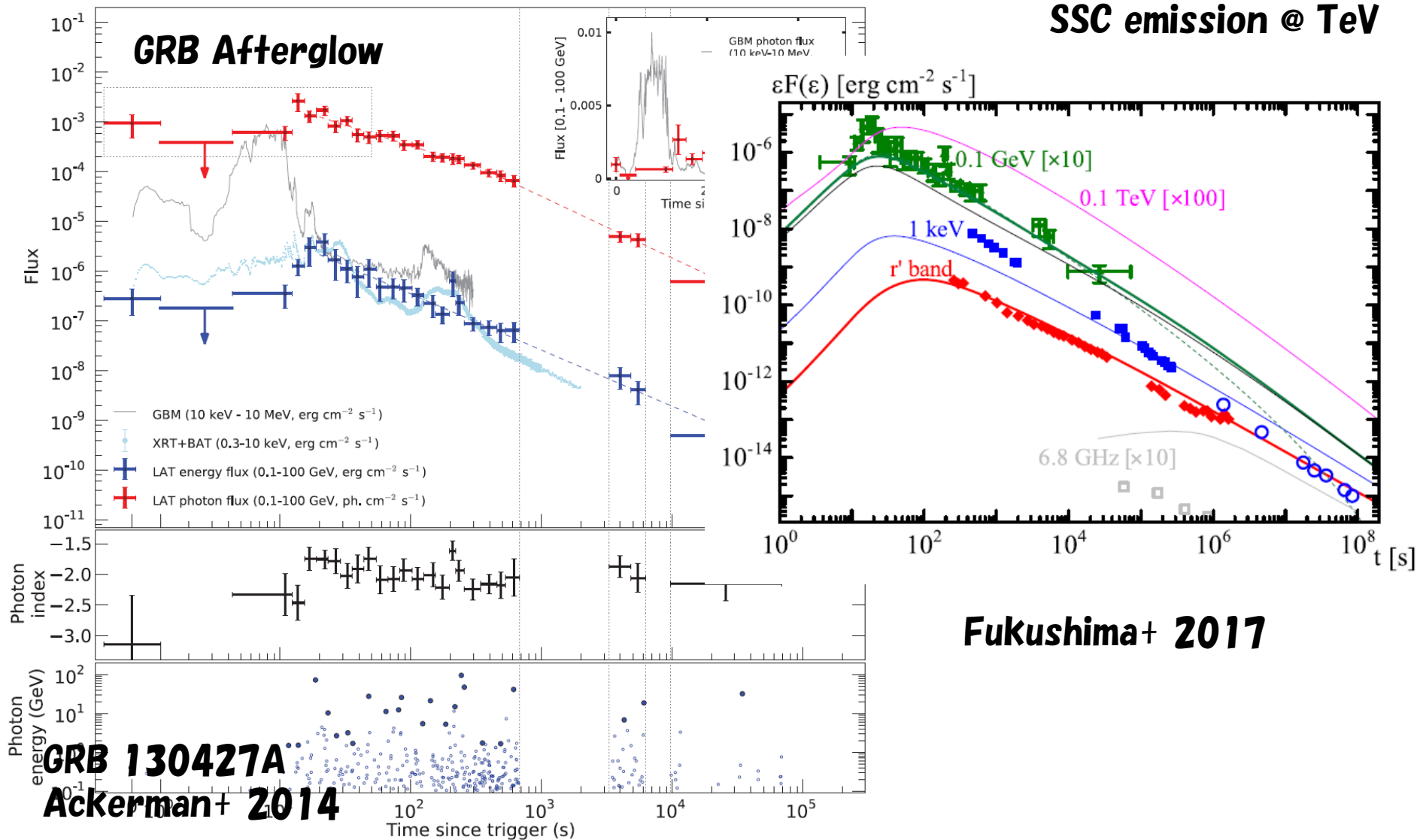


**Only above  $\sim 10^{20}$  eV**

**Asano & Meszaros 2014**

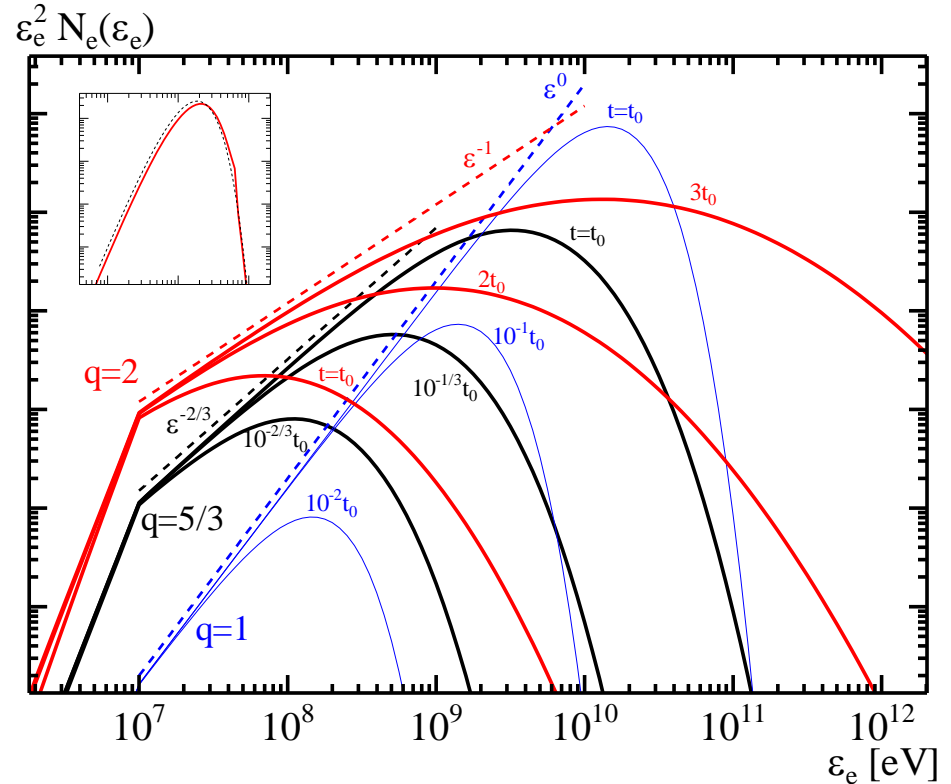
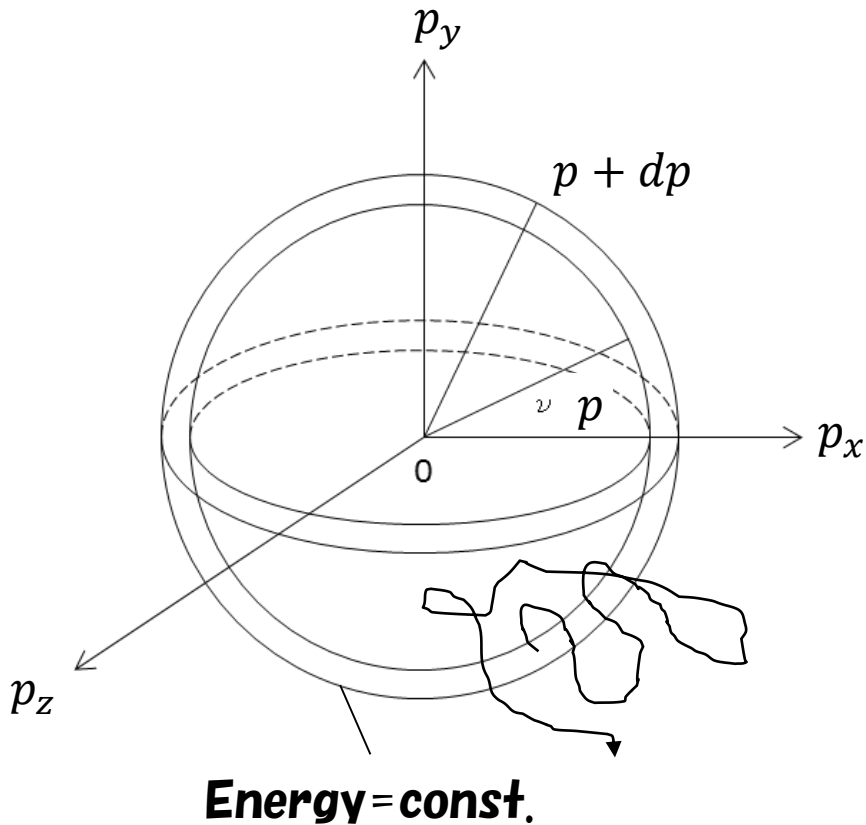
# Afterglow as calorimeter

SSC emission @ TeV



**Consistent with SSC by accelerated electrons at a relativistic shock!**  
**All non-thermal phenomena are due to shocks?**

# Stochastic acceleration by turbulence

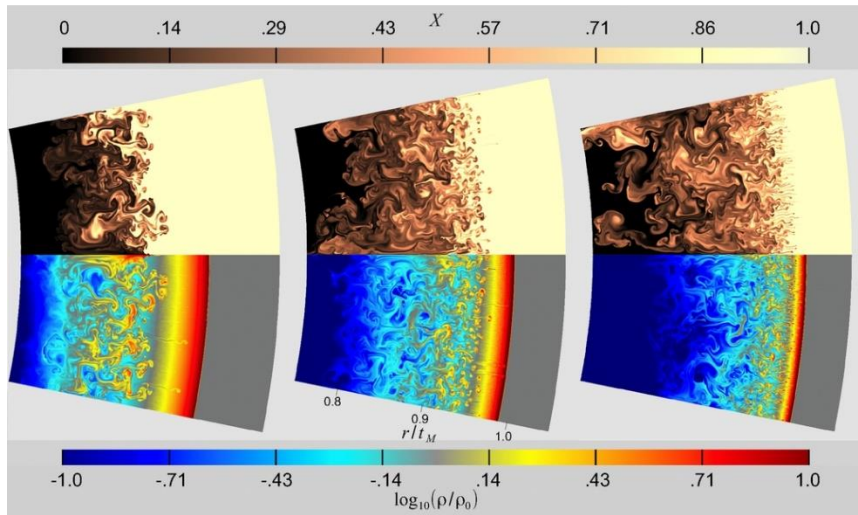


**Outer: larger volume  $\rightarrow$  Higher acceleration**

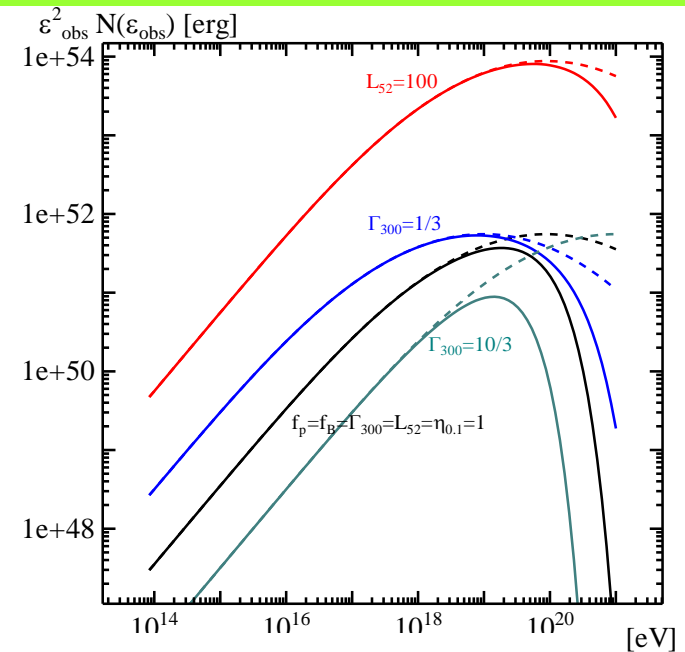
$$\frac{\partial N_e(\epsilon, t)}{\partial t} = \frac{\partial}{\partial E} \left[ \underbrace{D_{EE}}_{\text{Diffusion}} \frac{\partial N_e(E, t)}{\partial E} \right] - \frac{\partial}{\partial E} \left[ \left( \frac{2D_{EE}}{E} - \langle \dot{E}_{\text{cool}} \rangle \right) N_e(E, t) \right] + \dot{N}_{e,\text{inj}}(E, t)$$

**Diffusion**
**Acceleration**
**Cooling**
**Injection**

# UHECR production at the onset of GRB afterglow



Duffell and MacFadyen 2013



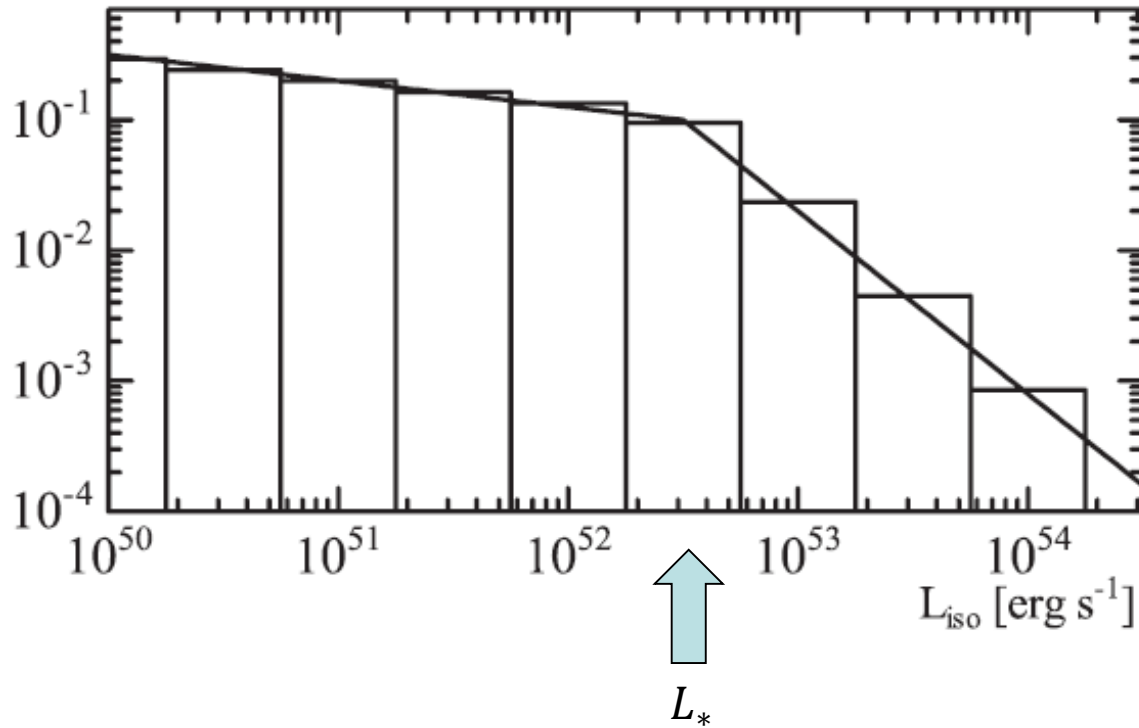
$$D_{EE} \propto E^2$$

$$\begin{aligned} \varepsilon_{\max} &= \frac{\xi e}{\Gamma} \sqrt{\frac{2f_B L_\gamma}{c}} \\ &\simeq 8.2 \times 10^{19} \xi_{0.1} \Gamma_{300}^{-1} f_B^{1/2} L_{52}^{1/2} \text{ eV} \end{aligned}$$

$$N_e(\varepsilon, t) = \frac{\text{Injection rate}}{6K\varepsilon_0} \frac{\dot{N}_{e,0} \varepsilon_0}{\varepsilon} \left[ 1 + \text{erf} \left[ \frac{3Kt - \ln \frac{\varepsilon}{\varepsilon_0}}{2\sqrt{Kt}} \right] - \left( \frac{\varepsilon}{\varepsilon_0} \right)^3 \text{erfc} \left[ \frac{3Kt + \ln \frac{\varepsilon}{\varepsilon_0}}{2\sqrt{Kt}} \right] \right]$$

**Diffusion coefficient**
**Elapsed time**

# GRB Luminosity function



**Progenitors (Ibc SN) seem common for low-luminosity GRBs and Fermi-LAT GRBs.**

$$L_{\text{tot}} = L_{\gamma} + L_B + L_{\text{CR}}$$

**is common?**

**With a constraint**

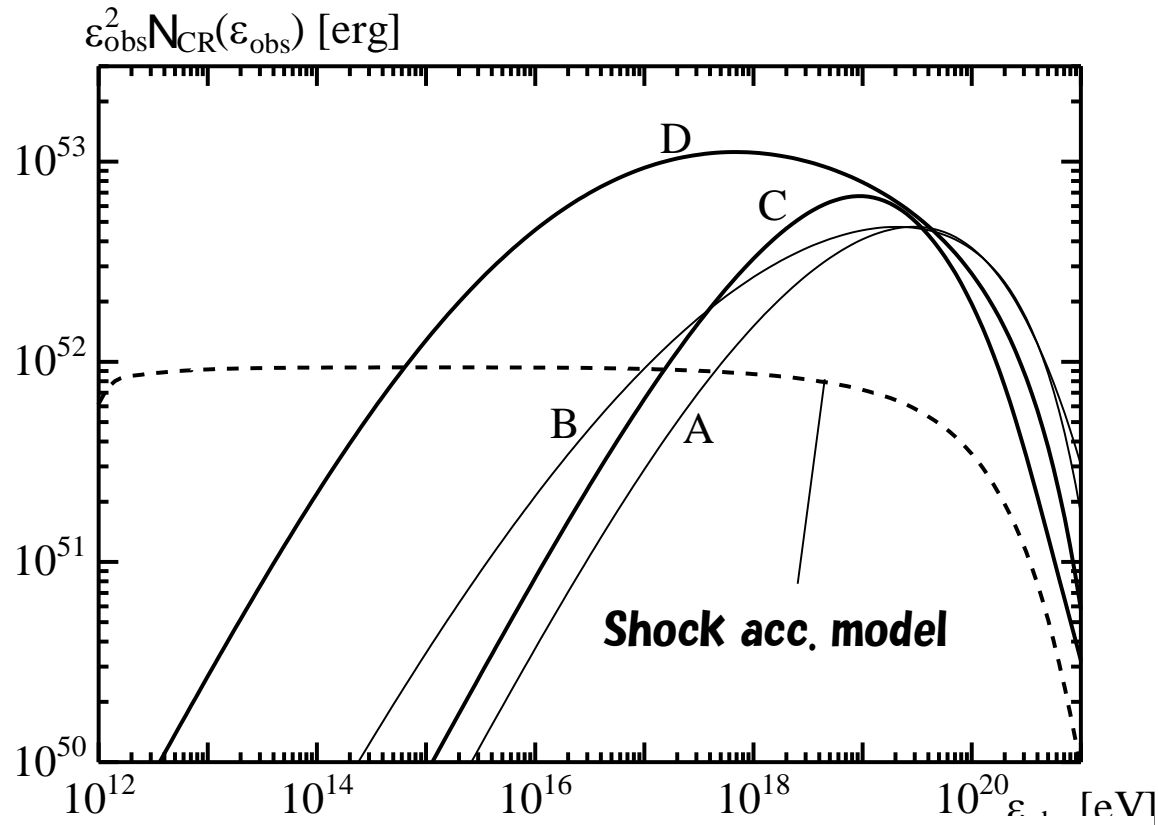
$$L_{\text{tot}} \leq 10L_*$$

**we adopt optimistic value of  $f_{\text{CR}}$  for dim GRBs.**

Model	A	B	C	D
$f_{\text{CR}}$	10	10	U.M. <sup>a</sup>	U.M.
$\Gamma$	300	$72.1L_{52}^{0.49}$	300	$72.1L_{52}^{0.49}$
LLC <sup>b</sup>	30.0%	45.8%	92.3%	100%

# Average UHECR spectrum for a GRB

$$L_{p,\text{typ}} = 10^{53.5} \text{ erg s}^{-1}$$



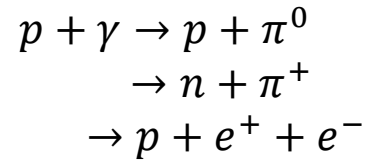
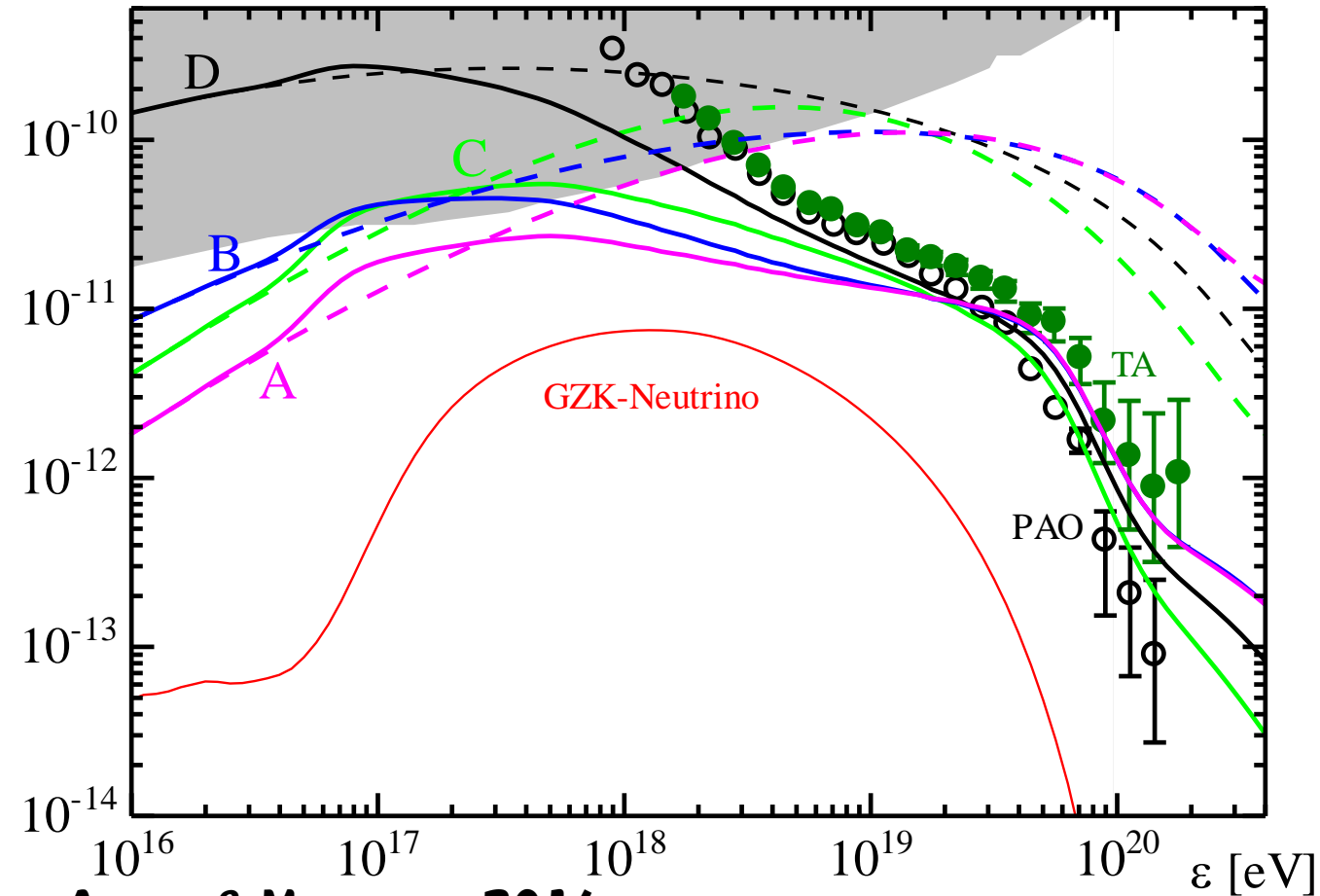
**Stochastic Acc. Model can concentrate UHECRs around the highest energy region.**

# Total UHECR Flux

Calculating the propagation of UHECRs

$\varepsilon^2 J(\varepsilon)$  [erg/cm<sup>2</sup>/s/sr]

1.3 Gpc<sup>-3</sup> yr<sup>-1</sup> above 10<sup>50</sup> erg s<sup>-1</sup>



Asano & Meszaros 2016

Seems possible as UHECR sources

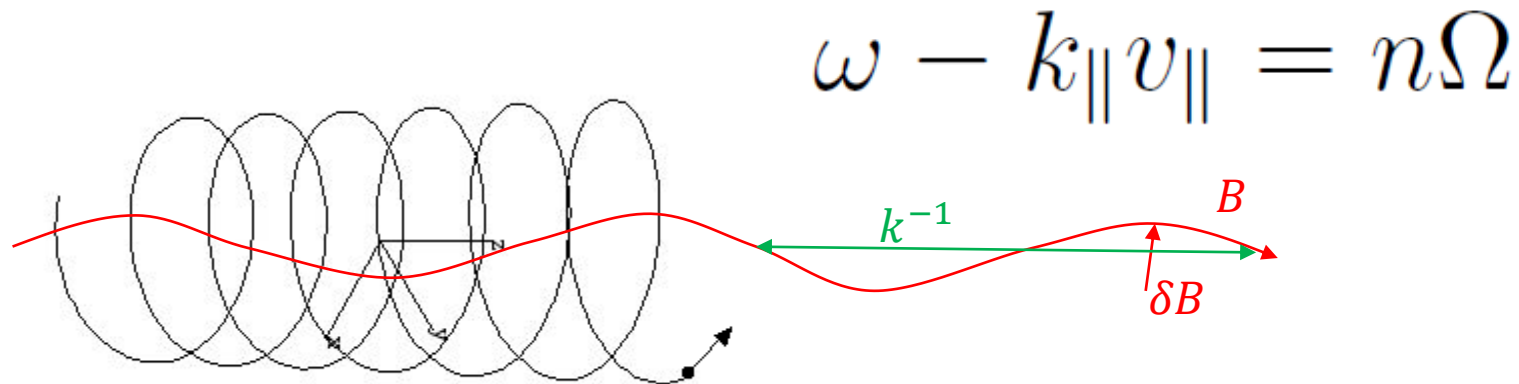


# Wave-Particle Interaction

**High-energy particles interact with macroscopic E-M waves.**

**Hereafter, we consider waves in MHD approximation.**

**The gyroresonance with Alfvén waves has been discussed.**



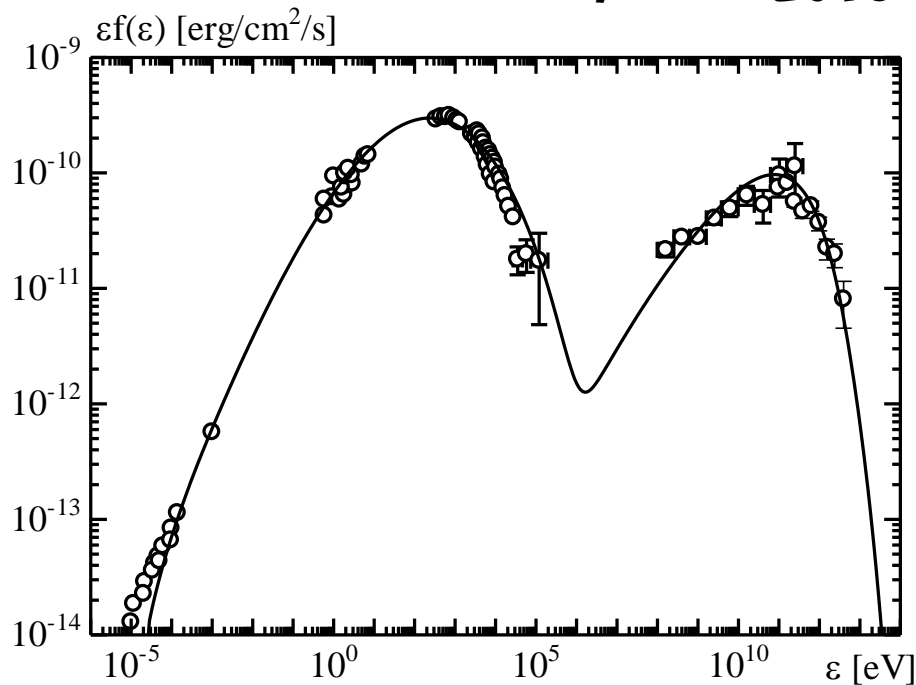
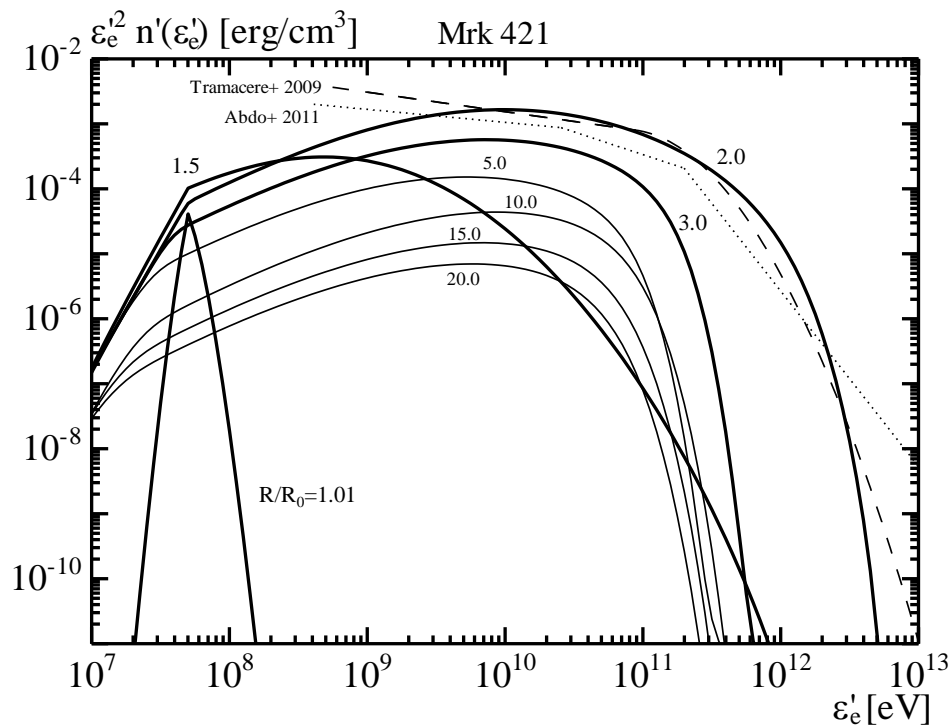
**The kinetic energy and magnetic energy in perturbation are comparable. But, the magnetic energy would be subdominant component.**

**Wave energy density**  $\delta B^2(k) \propto k^{-q} \rightarrow D_{EE} \propto E^q$

$q = 5/3$       **Kolmogorov case is standard.**

# Blazars suggest hard-sphere acceleration

Asano & Hayashida 2018



$$\Gamma = 15, B_0 = 0.16G, W' = \frac{R_0}{\Gamma} = 10^{16}\text{cm}, \Delta T'_{inj} = \frac{W'}{c}, K = 3.7 \times 10^{-6}\text{s}^{-1}, \dot{N} = 9.8 \times 10^{46}\text{s}^{-1}$$

$$t_{\text{coll}} \propto E^0, D_{EE} = KE^2$$

$U_B \ll U_e$  **The energy source would be not Alfvén waves.**

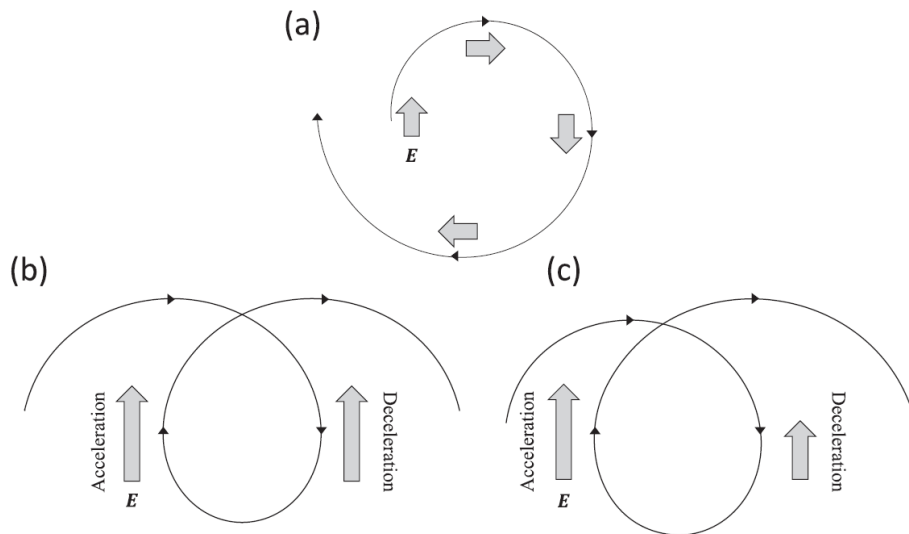
# Transit Time Damping

$$\omega - k_{\parallel} v_{\parallel} = n\Omega$$

**Compressible** MHD waves. Resonance with  $n = 0$ .

The parallel phase velocity is the same as the parallel particle velocity.

Essence: The electric field difference in one Gyro cycle.



Incompressible wave = Alfvén wave  
has no  $\nabla \times E \propto \delta B$  along  $B$ .  
No acceleration.

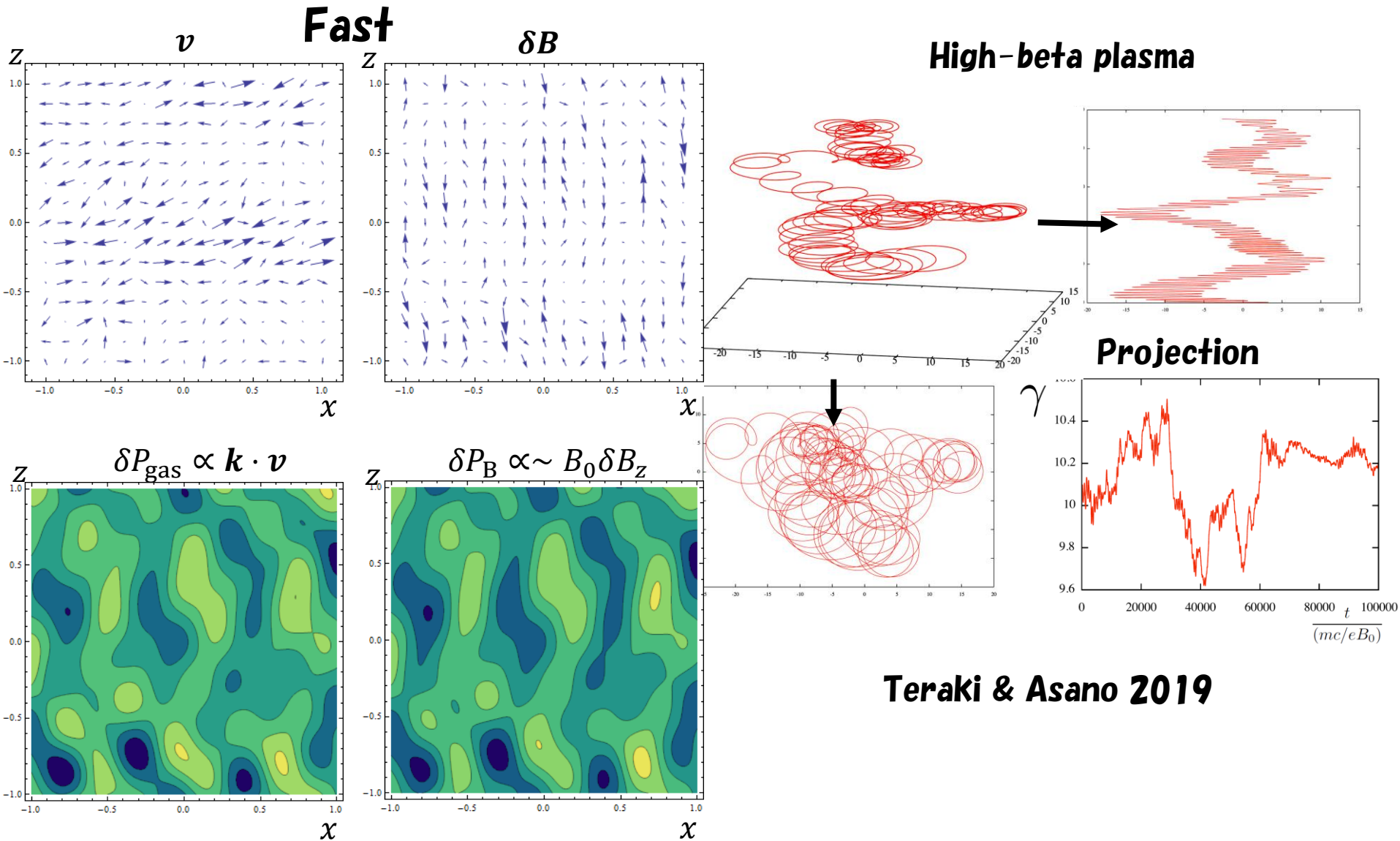
$k_{\perp}$  in compressible wave induces  
the change in  $E$

$$\text{When } r_L < k_{\max}^{-1}, \rightarrow D_{EE} \propto E^2$$

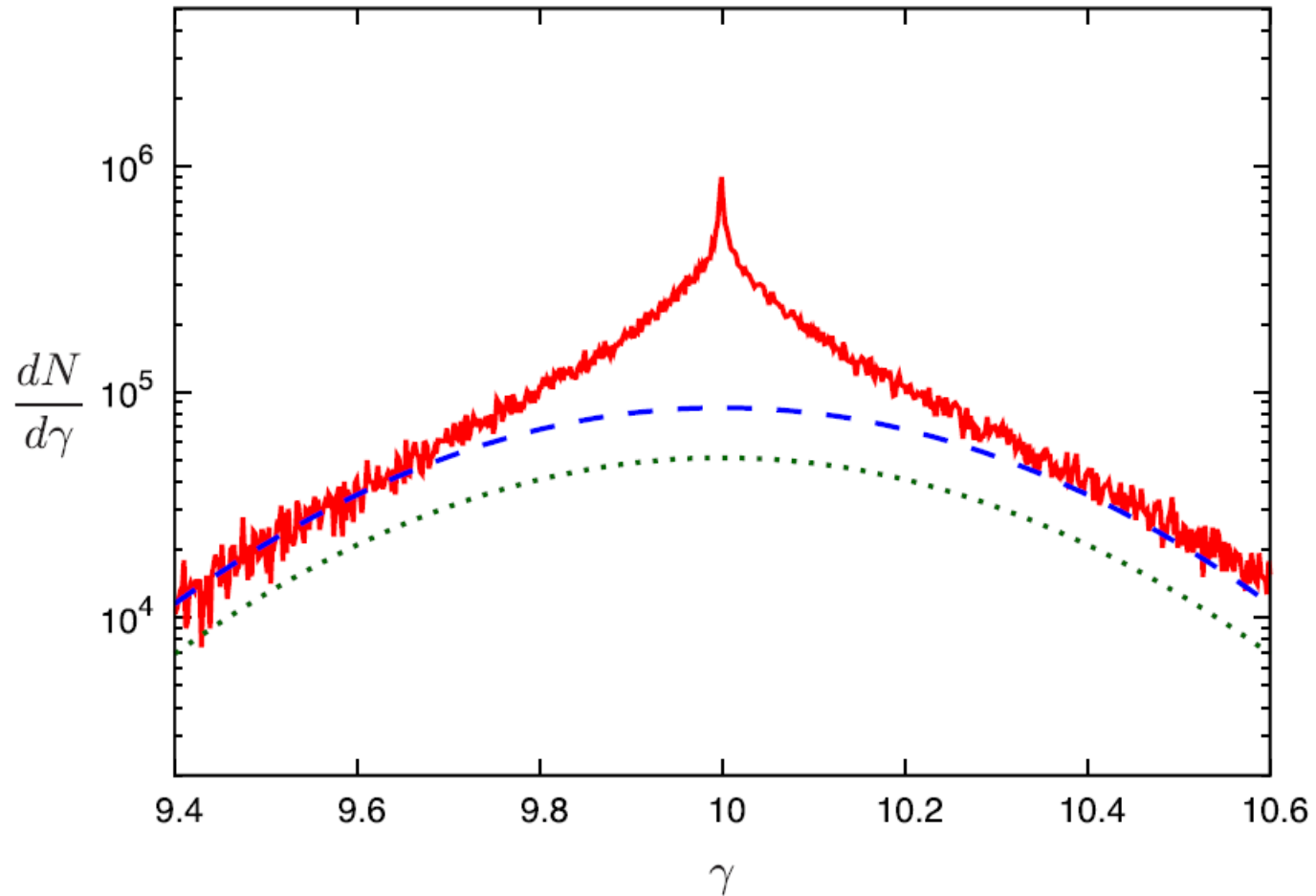
**Problem: The number fraction of accelerated particles is small?**

$$\text{Pitch angle } \cos\theta \sim \frac{v_{\parallel}}{c} \ll 1$$

# Test particle simulation in pure linear Waves



# Energy Diffusion



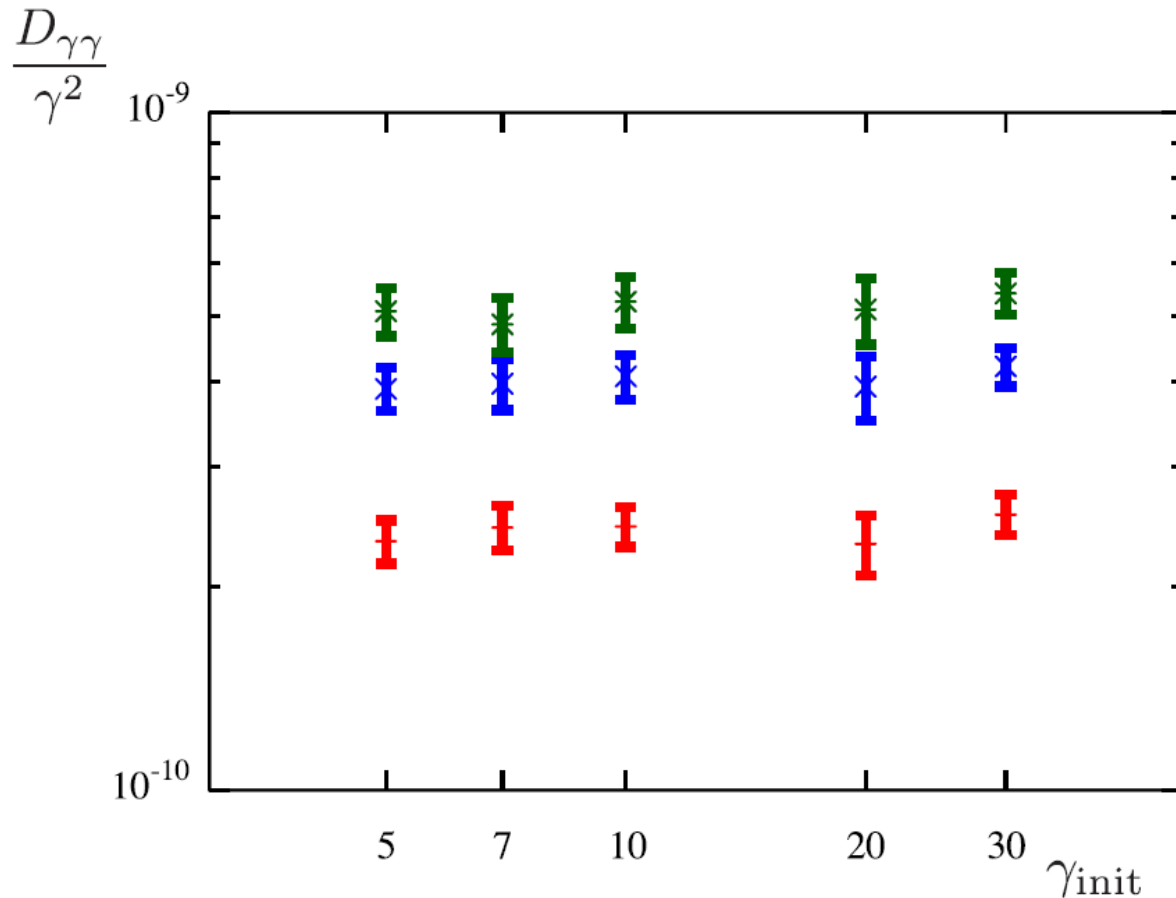
**Significant fraction of particles diffuses in the energy space.**

# Hard Sphere-like diffusion

When  $r_L < k_{\max}^{-1}$

$$D_{\gamma\gamma, \text{fast}} \sim \gamma^2 \left(\frac{V}{c}\right)^2 ck_{\max}(\nu - 1) \left(\frac{k_{\max}}{k_{\min}}\right)^{1-\nu} \epsilon_{\text{res,fast}}$$

$v_F = 0.1c, \delta V = 10^{-3}$  (**weak turb.**)



# Required Diffusion Coefficient

**Size of the acceleration region:  $R$**

**Diffusion Coefficient:  $D_{EE} = KE^2$**

**In our GRB-UHECR model, we consider the particle acceleration by eddy turbulence with a scale of  $\sim 0.1 R$ .**

**This corresponds to  $\frac{K}{c} \sim \frac{3}{R}$**

**With the turbulence velocity of  $c/\sqrt{3}$ ,  
if the fast-wave TTD is responsible, our simulation  
(Teraki & Asano 2019) shows**

$$\frac{K}{c} \sim 5.6 \frac{\pi}{18} \frac{1}{R} \left( \frac{R}{\lambda_{\min}} \right)^{2/3}$$

**$\lambda_{\min} \sim 0.1R$  is consistent with the above value.**

# Summary

- **A significant fraction of particles can resonate with fast waves via TTD.**
- **When the cut-off scale is larger than the Larmor radius, the hard-sphere acceleration realizes.**
- **UHECRs can be accelerated by turbulence at the onset of GRB afterglow.**
- **Since the acceleration timescale is long, electrons cool before accelerating.**
- **The required diffusion coefficient for UHECR production is not extreme one compared to our test particle simulation.**